# Quantum Music: Applying Quantum Theory to Music Theory and Composition

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Introduction: What is Music?

Music is a collection of sounds, or *tones*, that feature pitch, beat, and volume. Music consists of 3 elements:

- Melody: A set of musical notes, or tones, that are played in succession.
- **Harmony**: A set of musical notes that are played simultaneously.
- **Rhythm**: Duration of these sounds (or lack of sounds) in time.

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Traditionally, sounds called whole tones are represented as follows:



### CDEFGABC

For a single octave, all of the sounds used in music are represented by the *Chromatic scale*:



 $C C \ddagger D D \ddagger E F F \ddagger G G \ddagger A A \ddagger B$ 

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- Two elements of music notation that are used to denote pitch are b, the *flat* and \$\\$, the *sharp*.
- An alternate way to represent tones is by using the number 0 to represent no sound, and the numbers 1 − 12 as follows:
  C → 1, C ↓ → 2, D → 3, ..., A ↓ → 11, B → 12

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### How to quantize Music?

A quantum tone can be represented be a quantum musical state  $|\psi\rangle$ . A quantum musical state would be defined as:

$$|\psi\rangle = \alpha_0 |\psi_0\rangle + \alpha_1 |\psi_1\rangle + \alpha_2 |\psi_2\rangle + \ldots + \alpha_{12} |\psi_{12}\rangle \qquad (1)$$

With  $|\psi\rangle \in \mathbb{C}^{13}$  and  $\sum_{i} |\alpha_i|^2 = 1$ . Here,  $|\psi_i\rangle$  are the orthogonal unit vectors:

$$|\psi_{0}\rangle = \begin{pmatrix} 1\\0\\\vdots\\0 \end{pmatrix}, |\psi_{1}\rangle = \begin{pmatrix} 0\\1\\\vdots\\0 \end{pmatrix}, \dots, |\psi_{12}\rangle = \begin{pmatrix} 0\\0\\\vdots\\1 \end{pmatrix}$$

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We can also define a flat and sharp operators such that:

$$\hat{\flat} |\psi_i\rangle = \psi_{i-1} |\psi_{i-1}\rangle \tag{2}$$

$$\hat{\sharp} |\psi_i\rangle = \psi_{i+1} |\psi_{i+1}\rangle \tag{3}$$

## Melody: A simple example

# We start by constructing a simple system of two quantum tone states

$$\begin{split} |\psi\rangle_{1} &= \frac{1}{\sqrt{2}} |\psi_{0}\rangle + \frac{1}{\sqrt{2}} |\psi_{1}\rangle \qquad (4) \\ |\psi\rangle_{2} &= \frac{1}{\sqrt{2}} |\psi_{0}\rangle + \frac{1}{\sqrt{2}} |\psi_{1}\rangle \qquad (5) \end{split}$$

The system would have the following 4 possible outcomes, with equal probabilities:



Similarly for the following system quantum tone states,

$$\begin{split} |\psi\rangle_{3} &= \frac{1}{\sqrt{3}} |\psi_{0}\rangle + \frac{1}{\sqrt{3}} |\psi_{1}\rangle + \frac{1}{\sqrt{3}} |\psi_{6}\rangle \tag{6} \\ |\psi\rangle_{4} &= \frac{1}{\sqrt{3}} |\psi_{0}\rangle + \frac{1}{\sqrt{3}} |\psi_{1}\rangle + \frac{1}{\sqrt{3}} |\psi_{6}\rangle \tag{7} \end{split}$$

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The system would have the following 9 possible outcomes, with equal probabilities:



An advantage of this representation is that melodies can be composed by applying transformations, to tone states. In the previous example,

$$\left|\psi\right\rangle_{4} = \hat{1} \left|\psi\right\rangle_{3} \tag{8}$$

# Harmony: Entanglement?

Quantum Harmony can be thought as an entangled state of more than one quantum note, and could be represented using quantum chords.

Challenges and Future Work

- Incorporating rhythm.
- Incorporating volume.
- Finally, how to implement all of these ideas?

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